

EDEXCEL CORE MATHEMATICS C3 (6665)**MOCK PAPER MARK SCHEME**

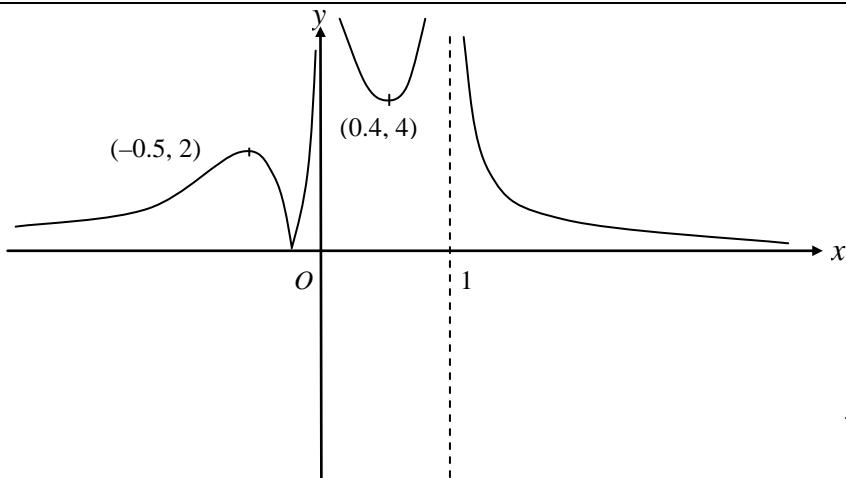
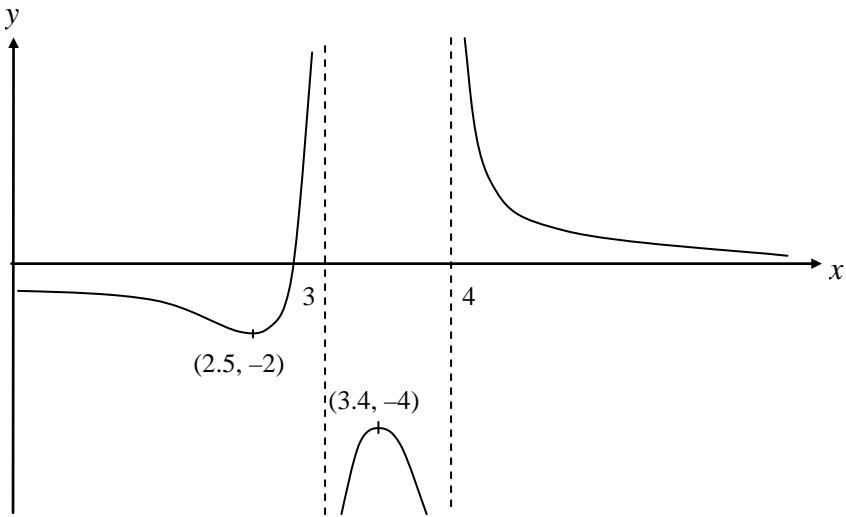
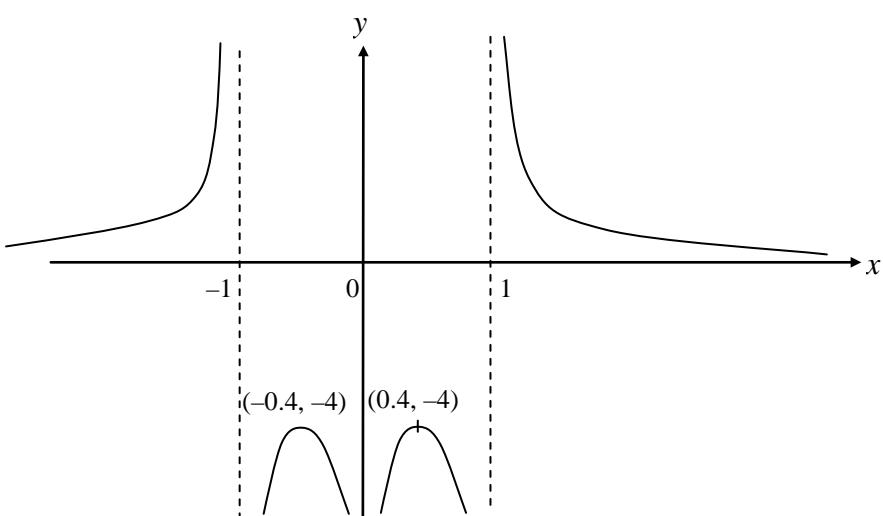
| Question number | Scheme | Marks |
|-----------------|---|--|
| 1. | $2x^2 + 7x + 6 = (x + 2)(2x + 3)$ $\frac{3x^2}{(2+x)(3+2x)} \times \frac{7(3+2x)}{3x^5}$ $= \frac{7}{(2+x)x^3}$ <p style="text-align: right;">some correct algebraic cancelling</p> | M1 A1 M1 A1 (4) (4 marks) |
| 2. (a) | $f^{-1}(x) = \frac{1}{2}x, \quad x \in \mathbb{R}$ | B1 B1 (2) |
| (b) | $gf^{-1}(x) = g(\frac{1}{2}x) = \frac{3}{4}x^2 + 2$ | M1 A1 (2) |
| (c) | Range $gf^{-1}(x) \geq 2$ | B1 (1) (5 marks) |
| 3. (i) | $e^{2x+3} = 6$ $2x + 3 = \ln 6$ $x = \frac{1}{2}(\ln 6 - 3)$ | M1 M1 A1 (3) |
| (ii) | $\ln(3x+2) = 4$ $3x + 2 = e^4$ $x = \frac{1}{3}(e^4 - 2)$ | M1 M1 A1 (3) (6 marks) |

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| 4. (i) | $u = x^3 \quad \frac{du}{dx} = 3x^2$ $v = e^{3x} \quad \frac{dv}{dx} = 3e^{3x}$ $\frac{dy}{dx} = 3x^2 e^{3x} + x^3 3e^{3x} \text{ or equiv}$ | M1 A1 A1 (3) |
| (ii) | $u = 2x \quad \frac{du}{dx} = 2$ $v = \cos x \quad \frac{dv}{dx} = -\sin x$ $\frac{dy}{dx} = \frac{2\cos x + 2x \sin x}{\cos^2 x} \text{ or equiv}$ | M1 A1 A1 (3) |
| (iii) | $u = \tan x \quad \frac{du}{dx} = \sec^2 x$ $y = u^2 \quad \frac{dy}{du} = 2u$ $\frac{dy}{dx} = 2u \sec^2 x$ $\frac{dy}{dx} = 2 \tan x \sec^2 x$ | M1 A1 (2) |
| (iv) | $u = y^2 \quad \frac{du}{dy} = 2y$ $x = \cos u \quad \frac{dx}{du} = -\sin u$ $\frac{dx}{dy} = -2y \sin y^2$ $\frac{dy}{dx} = \frac{-1}{2y \sin y^2}$ | M1 A1 M1 A1 (4) |
| | | (12 marks) |

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| 5. (a) (i) | $\begin{aligned} & \sin(A+B) - \sin(A-B) \\ &= \sin A \cos B + \sin B \cos A - \sin A \cos B + \sin B \cos A \\ &= 2 \sin B \cos A \quad (*) \end{aligned}$ | M1 A1 cso (2) |
| (ii) | $\begin{aligned} & \cos(A-B) - \cos(A+B) \\ &= \cos A \cos B + \sin A \sin B - \cos A \cos B + \sin A \sin B \\ &= 2 \sin A \sin B \quad (*) \end{aligned}$ | M1 A1 cso (2) |
| (b) | $\begin{aligned} & \frac{\sin(A+B) - \sin(A-B)}{\cos(A-B) - \sin(A+B)} = \frac{2 \sin B \cos A}{2 \sin A \sin B} \\ &= \frac{\cos A}{\sin A} \\ &= \cot A \quad (*) \end{aligned}$ | M1 A1 A1 cso (3) |
| (c) | $\begin{aligned} & \text{Let } A = 75^\circ \text{ and } B = 15^\circ \\ & \frac{\sin 90^\circ - \sin 60^\circ}{\cos 60^\circ - \cos 90^\circ} = \cot 75^\circ \\ & \cot 75^\circ = \frac{1 - \frac{\sqrt{3}}{2}}{\frac{1}{2} - 0} = 2 - \sqrt{3} \end{aligned}$ | B1 M1 M1 A1 (4) (11 marks) |

| Question number | Scheme | Marks |
|-----------------|--|---|
| 6. (a) |  <p>$x < 0$ $0 < x < 1$ $x > 1$</p> | B1 shape B1 shape B1 shape B1 points (4) |
| (b) |  | M1 any translation M1 correct direction, translation B1 points B1 asymptotes (4) |
| (c) |  | B1 shape > 0 B1 shape < 0 B1 points B1 asymptotes (4) |
| | | (12 marks) |

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| 7. (a) | <p>$y = \ln x$</p> | B1 shape B1 x -intercept labelled (2) |
| (b) | $\frac{dy}{dx} = \frac{1}{x}$ so tangent line to $(e, 1)$ is $y = \frac{1}{e}x + C$ the line passes through $(e, 1)$ so $1 = e\frac{1}{e} + C$ and $C = 0$ The line passes through the origin. | M1 M1 A1 (3) |
| | | |
| (c) | All lines $y = mx$ passing through the origin and having a gradient > 0 lie above the x -axis. Those having a gradient $< \frac{1}{e}$ will lie below the line. $y = \frac{x}{e}$ so it cuts $y = \ln x$ between $x = 1$ and $x = e$. | B1 B1 (2) |
| (d) | $x_0 = 1.86$ $x_1 = e^{\frac{x_n}{3}} = 1.859$ $x_2 = 1.858$ $x_3 = 1.858$ $x_4 = 1.858$ $x_5 = 1.857$ | M1 A1 A1 A1 A1 (3) |
| (e) | When $x = 1.8575$, $\ln x - \frac{1}{3}x = 0.000\ 064\ 8\dots > 0$ When $x = 1.8565$, $\ln x = -0.000\ 140\dots < 0$ Change of sign implies there is a root between. | M1 A1 A1 (3) |
| | | (13 marks) |

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|-----------------|--|--|
| 8. (a) | $4 \sin \theta - 3 \cos \theta = R \sin \theta \cos \alpha - R \cos \theta \sin \alpha$ sin θ terms give $4 = R \cos \alpha$ cos θ terms give $3 = R \sin \alpha$ $\tan \alpha = 0.75$ $\alpha = 36.9^\circ$ $R^2 = 4^2 + 3^2 = 25 \Rightarrow R = 5$ | M1 A1 M1 A1 (4) |
| (b) | $5 \sin (\theta - 36.9^\circ) = 3$ $\sin (\theta - 36.9^\circ) = 0.6$ $\theta - 36.9^\circ = 36.9^\circ, 143.1$ $\theta = 73.7^\circ, 180^\circ$ | M1 A1 M1 awrt 74° A1 A1 (5) |
| (c) | Max value 5 | B1 (1) |
| (d) | $\sin (\theta - 36.9^\circ) = 1$ $\theta - 36.9^\circ = 90^\circ$ $\theta = 90^\circ + 36.9^\circ = 126.9^\circ$ | M1 A1 (2) |
| | | (12 marks) |

| Question | Specification Section | AO1 | AO2 | AO3 | AO4 | AO5 | Totals |
|-----------------|------------------------------|------------|------------|------------|------------|------------|---------------|
| Q1 | 1.1 | 2 | 2 | | | | 4 |
| Q2 | 1.2 | 3 | 2 | | | | 5 |
| Q3 | 3.1, 3.2 | 2 | 4 | | | | 6 |
| Q4 | 4.1, 4.2, 4.3 | 5 | 6 | | | 1 | 12 |
| Q5 | 2.3 | 3 | 5 | | 3 | | 11 |
| Q6 | 1.3, 1.4 | 7 | 5 | | | | 12 |
| Q7 | 3.2, 5.2 | 2 | 3 | 2 | 3 | 3 | 13 |
| Q8 | 2.1, 2.3 | 2 | 2 | 3 | 2 | 3 | 12 |
| | TOTAL | 26 | 29 | 5 | 8 | 7 | 75 |